LIST OF NOTATIONS

| Symbols | Definition |
|-----------------|---|
| V | Vertex set $\{v_0, v_1, \dots, v_n\}$ |
| E | Edge set $\{(v_i, v_j) v_i, v_j \in V, i \neq j\}$ |
| v_i | Vertex i (hotel if $i = 0$, POI if $i \ge 1$) |
| S | User's desired hotel and POIs set |
| D | Travel day set |
| Q | Daily travel duration limit |
| Q_0 | Departure time |
| Q_1 | Time limit for returning to hotel |
| Oi | Opening hour of v_i |
| c_i | Closing hour of v_i |
| N | Maximum number of travel days |
| t_{ij} | Travel time from v_i to v_j |
| wt_i | Waiting time at v_i |
| s_i | Time spent on v_i |
| at_i | Arrival time at v_i |
| $rating_i$ | Rating of v_i |
| $cost_i$ | Cost of v_i |
| Т | Total travel duration |
| T_d | Travel duration on day d |
| x_i | Value of attribute i |
| $x_{i_{max}}$ | Maximum value of attribute i |
| $x_{i_{min}}$ | Minimum value of attribute i |
| $x_{i_{norm}}$ | Normalized value of attribute i |
| $U(x)_{norm}$ | Multi-Attribute Utility Theory (MAUT) value with the normalized |
| | attributes |
| w_i | Degree of interest (DOI) of attribute i |
| q_0 | Probability parameter for transition rule in Ant Colony System |
| | (ACS) |
| $J_k(i)$ | The subset of set V that is still possible to be visited by ant k |
| $	au_{ij}$ | Pheromone concentration along the path from v_i to v_j |
| η_{ij} | Heuristic value from v_i to v_j , equivalent to $U_j(x)_{norm}$ |
| $U_j(x)_{norm}$ | MAUT value for v_j considering attributes such as the cost and rating |
| | of v_j , along with the travel time from v_i to v_j |
| αt | Relative influence of τ_{ij} |
| β | Relative influence of η_{ij} |

| Symbols | Definition |
|----------------------|--|
| ρ | Pheromone evaporation rate within the range of $[0,1]$ for local |
| | pheromone update |
| $U(x)_{norm_k}$ | Fitness value by ant k |
| α | Pheromone evaporation rate for global pheromone update |
| $U(x)_{norm_{best}}$ | Fitness value for the best solution |